On the comparison of the Fridman invariant and the squeezing function

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Abstract

Fridman invariant and squeezing function have attracted much attention in recent years. Since they are similar in spirit to the Kobayashi-Eisenman volume form K_D and the Caratheodory volume form C_D , it is a natural problem to consider the comparison of these two biholomorphic invariants.

Let's consider a quotient $m_D(z) = \frac{s_D(z)}{e_D(z)}$ where $s_D(z)$ and $e_D(z)$ are squeezing function and Fridman invariant respectively. We study the following two questions:

- 1) If $m_D(z_0) = 1$ for some $z_0 \in D$, is D biholomorphic to the unit ball?
- 2) Is $m_D(z)$ constantly equal to 1?